



ST. XAVIER'S COLLEGE, MAPUSA GOA

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Nature of Event (Workshop, Guest Lecture, Add-on Course, Seminar, etc.)	Summer school
Name of Department	Mathematics
Faculty In-Charge	Mr. Rahul Naik
Stratum of Event (College, State, Regional, National)	State
Title of Event	Summer school on Linear Algebra
Date of Event	24 March 2022 to 26 March 2022
Venue	Online
Resource Person details	Mr. Prashant Kumar Singh Tata Institute of fundamental Research, Bangalore, Karnataka.
Objective/ Scope of Event	The objective of this program was to review and learn some advanced linear algebra concepts which would help participants in answering the entrance and other competitive examinations related to mathematics.
Particulars of Event	<p>The Department of Mathematics, St. Xavier's College, Mapusa-Goa organized Summer School in Mathematics on the topic "Linear Algebra- Diagonalization of Matrices".</p> <p>The session started with recalling the basic concept of linear algebra namely vector spaces by the resource person. He then introduced the notion of Algebra over a field F, followed by showing the relation between Lagrange's polynomial and Kronecker delta function. He also introduced the notion of polynomial ideals. Sir then explained the concepts of elementary canonical form of a matrix, matrix representation of linear transformation, diagonalizable operator, similar matrices and algebraically closed field.</p> <p>The second session started with introduction of Independent subspaces by the resource person, followed by proving some important results. Concepts such as Invariant subspaces, Introduced linear operators and their matrix representations, Block matrices were beautifully explained following the proof of related theorems. In the third session the resource person started with proving results on diagonalizable operator. Sir discussed the concepts of Annihilating polynomials space, minimal polynomial and some very important results on similar matrices, characteristic and minimal polynomials and diagonalizable operator. At last he</p>

	introduced the notion of conductor of an element in vector subspace and proved that it is an ideal in $F[x]$. Using the notion of conductor, one can easily obtain results on simultaneous triangularization and diagonalization of classes of matrices.
Outcome of Event	Students will be able to find characteristic polynomial and minimal polynomial of a matrix, find eigen values and eigen vectors of a matrix, Perform diagonalization of matrices, Explain the significance of diagonalization of matrices, check if the linear operator is diagonalizable or not, find determinant of block triangular matrices and prove that similar matrices have same minimal polynomial.
Feedback	Participants appreciated the Lecture and it was very refreshing.

Total No. of Participants

33

Photographs

Lagrange Polynomial in $F[x]$

$x_1, x_2, \dots, x_n \in F$

$$P_i = \prod_{j \neq i} \frac{(x - x_j)}{(x_i - x_j)}$$

$F = \mathbb{R}, \quad x_1 = 1, \quad x_2 = 2, \quad x_3 = 3$

$P_1(x) = 0x$

$$P_1 = \frac{(x - x_2)(x - x_3)}{(x_1 - x_2)(x_1 - x_3)} = \frac{(x - 2)(x - 3)}{(1 - 2)(1 - 3)} = \frac{(x - 2)(x - 3)}{-1 \cdot -2} = \frac{(x - 2)(x - 3)}{2}$$
$$P_2 = \frac{(x - 1)(x - 3)}{(2 - 1)(2 - 3)}$$
$$P_3 = \frac{(x - 1)(x - 2)}{(3 - 1)(3 - 2)}$$

Characteristic values

Let V be a vector space over a field F .
Let $T \in \mathcal{L}(V, V)$
 $\alpha \in F$ is called characteristic value if
 $\exists \alpha \in V, \alpha \neq 0$ s.t.
 $T\alpha = \alpha$

$T: V \rightarrow V$

$\dim V = n$
 $\mathcal{L}(V, V) =$ space of linear operators on V
 $\mathcal{L}(V, V)$ is VS.
 $\dim \mathcal{L}(V, V) = n^2$

People

Share invite

Currently in this meeting (44)

- SB Swapnil Belekar (Guest)
- AS Anchal Arun Sawant
- AV Arianne Lira Vas
- CC Callista Valanka Cabral
- GN Gulshan Shyamsunder Nishad
- JM Jovi Moura
- MT Manasi Mukund Talavdekar
- MF Meryl Fernandes
- MP Mr. Gajanan Rama Parab
- MN Mr. Rahul Naik

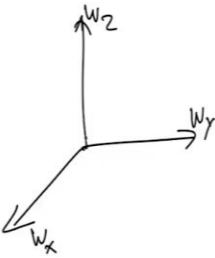
characteristic polynomial - OneNote

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Maths Works > New Section 1

Independent Subspace

Definition Let W_1, W_2, \dots, W_k be subspaces in V .
 V is a vector space over F .
 We say W_1, W_2, \dots, W_k are independent
 if $\alpha_1 + \alpha_2 + \dots + \alpha_k = 0, \alpha_i \in W_i$
 $\Rightarrow \alpha_i = 0$



24:48

32°C Prashant Singh (Guest)

People

Share invite

Currently in this meeting (39)

- SG Shreyash Rajesh Govekar
- SR Shubhang Sandesh Rege
- SG Sonam Sadguru Godkar
- SR Swanit Nitin Rivankar
- SM Sweta Vasant Malik
- TT Tanaya Mahesh Talkar
- TP Tanmay Raghoba Parab
- VP Vibhav Tulshidas Pal
- V vikita (Guest)
- VD Vinita Sunil Diukar

+33 GN OM MT MN PS

Manasi Mukund Tala... Mr. Rahul Naik prashant Singh (Guest)



prashant Singh (Guest) Mr. Rahul Naik Swapnil Belekar (Guest) Rohan Daivajna

Zen Lobo Balakrishnan Nair Mr. Gajanan Rama Parab Shambhavi Avinash Manerikar

Sonam Sadguru Godkar Omkar Daji Chavan

Mute

02:22:46

BN MN PS

Balakrishnan Nair (G... Mr. Rahul Naik prashant Singh (Guest)

